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**PAPER**

Temporally and spectrally multiplexed single photon source using quantum feedback control for scalable photonic quantum technologies

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Mikkel Heuck^{1,2} , Mihir Pant² and Dirk R Englund²¹ Department of Photonics Engineering, Technical University of Denmark, Building 343, DK-2800 Kgs. Lyngby, Denmark² Department of Electrical Engineering and Computer Science, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, MA 02139, United States of AmericaE-mail: mheu@fotonik.dtu.dk and englund@mit.edu**Keywords:** single photon source, quantum feedback control, quantum information technology**Abstract**

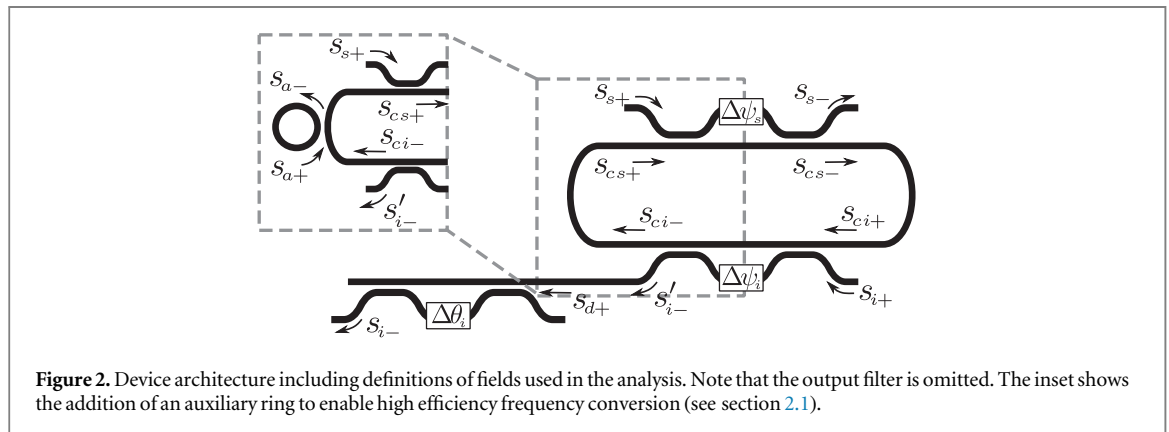
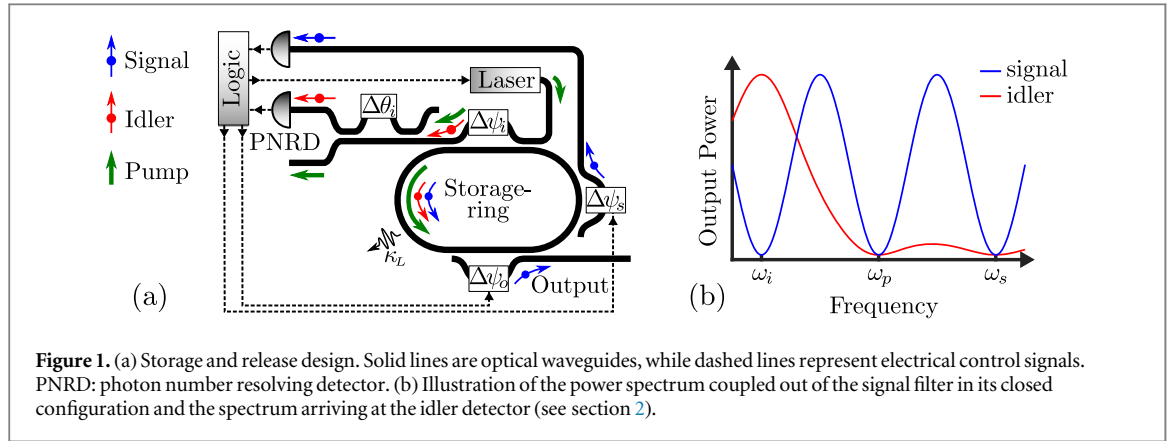
Current proposals for scalable photonic quantum technologies require on-demand sources of indistinguishable single photons with very high efficiency. Even with recent progress in the field there is still a significant gap between the requirements and state of the art performance. Here, we propose an on-chip source of time-multiplexed, heralded photons. Using quantum feedback control on a photon storage cavity with an optimized driving protocol, we estimate an on-demand efficiency of 99% and unheralded loss of order 1%, assuming high efficiency detectors and intrinsic cavity quality factors of order 10^8 . We further explain how temporal- and spectral-multiplexing can be used in parallel to significantly reduce device requirements if single photon frequency conversion is possible with efficiency in the same range of 99%.

1. Introduction

Achieving sources of on-demand pure single photon states has been a long-standing goal of quantum information science [1]. Recent years have seen considerable progress in the performance of ‘deterministic sources’ based on two-level quantum emitters [2–4]. Additionally, the efficiency of sources based on probabilistic processes, such as parametric down-conversion and spontaneous four-wave mixing (sFWM), has been improved by multiplexing either spatial [5], temporal [6, 7], or spectral [8] degrees of freedom of photons. Despite this progress, a large gap remains between state-of-the-art demonstrations and the requirements of proposed quantum information processing technologies, including photonic quantum repeaters [9], precision sensors [10], and photonic quantum computing [11, 12]. We believe this calls for investigations into novel device concepts that are necessary to bridge this gap.

In this work, we investigate the feasibility of single photon sources that meet the requirements of scalable photonic quantum technologies: near-unity purity single photons produced in a reproducible chip-integrated photonic circuit. Our proposal uses temporal multiplexing of parametrically produced signal-idler photon pairs and includes the possibility of additional multiplexing of the spectral degree of freedom leading to significantly improved performance.

We consider a control protocol based on Bayesian inference with both idler and signal photon detection to optimize the signal photon state. This approach shows the trade-off between heralding the generation of a single photon state and its purity. Our study reveals that, for near-term realistic device parameters, highly efficient ($\sim 99\%$) sources of single photons could be possible in scalable nanophotonic platforms. As illustrated in figure 1 (a), our proposed device consists of a high Q microring resonator (Q of 10 – 100 million) consisting of a material, such as silicon, with a $\chi^{(3)}$ nonlinearity for photon pair generation by sFWM. This storage ring is coupled to photon number resolving detectors through Mach–Zehnder interferometer (MZI) filters [13]. The filters enable decoupling of certain frequencies from the waveguide by controlling the path-imbalance of the



MZI relative to the length of the ring (see figure 1(b)). Idler photons and the pump field couple out of the storage ring within a single time bin, whereas the signal can be stored for up to M bins. The signal- and output filters contain tunable phases, $\Delta\psi_s(t)$ and $\Delta\psi_o(t)$, allowing them to dynamically couple out signal photons to a detector or output waveguide, respectively. Each emission cycle is divided into M time bins in which we either: (1) pump to generate a photon pair; (2) release excess signal photons by tuning the phase of the signal filter; (3) evacuate all photons from the system through the signal filter; or (4) store the signal state if detection events suggest a single photon is present. The driving protocol prescribes which action is taken in a given time bin depending on the information available from detection events. We optimize the protocol to maximize the probability of a single signal photon occupying the storage ring at the emission time, t_M . Signal photons are emitted by tuning the output filter to its open state. Tailoring the temporal shape of $\Delta\psi_o(t)$ allows shaping the output photon wavepacket. Note that decoupling the signal mode from the environment reduces the spectral correlations of the signal-idler quantum state, which increases the purity of the single photon state of the signal after detecting the idler.

This article is organized as follows: section 2 details the device architecture and explains how multiplexing in both time and frequency is possible. Sections 3 and 4 present the model and probability analysis for evaluating the performance of our proposed architecture and section 5 discusses the driving protocol. Section 6 presents simulation results and section 7 concludes with a discussion of the feasibility of experimental demonstrations.

2. Device architecture

Our proposed device implementation uses a photonic integrated circuit consisting of a ring resonator and MZI-couplers [13], as illustrated in figure 1(a). The structure is shown again in figure 2 with definitions of fields used in the analysis.

The outputs of the MZI filters are related to the inputs by

$$\begin{bmatrix} s_{n-} \\ s_{cn-} \end{bmatrix} = C^{(n)} Z^{(n)} C^{(n)} \begin{bmatrix} s_{n+} \\ s_{cn+} \end{bmatrix}, \quad n = \{i, s\}, \quad (1)$$

where $n = \{i, s\}$ represent the idler and signal filter. The matrices $\mathbf{C}^{(n)}$ and $\mathbf{Z}^{(n)}$ are given by

$$\mathbf{C}^{(n)} = \begin{bmatrix} \nu_n & i\sqrt{1-\nu_n^2} \\ i\sqrt{1-\nu_n^2} & \nu_n \end{bmatrix}, \mathbf{Z}^{(n)} = \begin{bmatrix} e^{i\psi_{nT}} & 0 \\ 0 & e^{i\psi_{nB}} \end{bmatrix}, \quad (2)$$

where ψ_{nT} and ψ_{nB} are the phase accumulation in the arm containing the phase shifter and the arm that is part of the ring, respectively. The through-coupling of the waveguide couplers is ν_n . The transfer matrix $\mathbf{T}^{(n)} = \mathbf{C}^{(n)}\mathbf{Z}^{(n)}\mathbf{C}^{(n)}$ of the MZI filter is

$$\mathbf{T}^{(n)} = e^{i\psi_{nB}} \begin{bmatrix} (1 + e^{i\psi_n})\nu_n^2 - 1 & i(1 + e^{i\psi_n})\nu_n\sqrt{1-\nu_n^2} \\ i(1 + e^{i\psi_n})\nu_n\sqrt{1-\nu_n^2} & \nu_n^2 - e^{i\psi_n}(1 - \nu_n^2) \end{bmatrix}, \quad (3)$$

where $\psi_n = \psi_{nT} - \psi_{nB}$ is the difference in phase accumulation between the two arms. We assume that the phases $\Delta\psi_n$ are tunable such that

$$\psi_n(\omega) = k(\omega)\Delta L_n + \Delta\psi_n, \quad n = \{i, s\}. \quad (4)$$

Here, the path length difference between the MZI arms is ΔL_n and the propagation constant is approximated as

$$k(\omega) \approx \frac{\tilde{n}_{\text{eff}}}{c}\omega_0 + \frac{n_g}{c}(\omega - \omega_0), \quad (5)$$

where the complex effective mode index is $\tilde{n}_{\text{eff}} = n'_{\text{eff}} + in''_{\text{eff}}$ and the group index is defined from $n_g/c \equiv \partial k/\partial\omega$.

As mentioned in section 1 the filters must be designed to only allow certain frequencies to pass. To illustrate how this may be accomplished let us consider a situation where a field, s_f , is generated inside the ring between the signal and idler filter, such that

$$s_{ci+} = e^{i\phi_{si}}s_{cs-} + s_f, \quad s_{s+} = s_{i+} = 0. \quad (6)$$

The fields are related using figure 2 and equation (3)

$$s_{ci+} = e^{i\phi_{si}}T_{2,2}^{(s)}s_{cs+} + s_f = e^{i\phi_{si}}T_{2,2}^{(s)}e^{i\phi_{is}}s_{ci-} + s_f = e^{i\phi_{si}}T_{2,2}^{(s)}e^{i\phi_{is}}T_{2,2}^{(i)}s_{ci+} + s_f, \quad (7)$$

where $T_{i,j}^{(n)}$ is the matrix element of $\mathbf{T}^{(n)}$ corresponding to the i th row and j th column. The round-trip phase of the isolated storage ring is

$$\phi_c(\omega) = \psi_{iB} + \phi_{is} + \psi_{sB} + \phi_{si} = k(\omega)L_c, \quad (8)$$

where L_c is the length of the storage ring. From equation (7), we have

$$s_{ci+} = \frac{1}{1 - e^{i\phi_c}\zeta_i\zeta_s}s_f, \quad (9)$$

where ζ_n is a tuning parameter of the ring-waveguide coupling given by

$$\zeta_n \equiv T_{2,2}^{(n)}e^{-i\psi_{nB}} = \nu_n^2 - e^{i\psi_n}(1 - \nu_n^2). \quad (10)$$

The out-going fields are given by

$$s_{s-} = T_{1,2}^{(s)}s_{cs+} = \frac{T_{1,2}^{(s)}e^{i\phi_{is}}T_{2,2}^{(i)}}{1 - e^{i\phi_c}\zeta_i\zeta_s}s_f, \quad s_{i-} = D_{1,2}^{(i)}s'_{i-} = \frac{D_{1,2}^{(i)}T_{1,2}^{(i)}}{1 - e^{i\phi_c}\zeta_i\zeta_s}s_f. \quad (11)$$

The drop filter transfer matrix is

$$\mathbf{D}^{(i)} = e^{i\theta_{iB}} \frac{1}{2} \begin{bmatrix} e^{i\theta_i} - 1 & i(1 + e^{i\theta_i}) \\ i(1 + e^{i\theta_i}) & 1 - e^{i\theta_i} \end{bmatrix}. \quad (12)$$

The through-coupling coefficient, ν_m , from equation (2) was chosen to be $1/\sqrt{2}$ in equation (12) to achieve 100% visibility of the drop filter. The phase difference between the arms is

$$\theta_i(\omega) = k(\omega)\Delta L_{di} + \Delta\theta_i. \quad (13)$$

The idler, pump, and signal frequencies are chosen from three adjacent modes of the storage ring, such that

$$\omega_i = \omega_p - \Omega_c, \quad \omega_s = \omega_p + \Omega_c, \quad (14)$$

where Ω_c is the free spectral range (FSR) of the storage ring. From the out-coupling matrix elements

$$T_{1,2}^{(n)} = T_{2,1}^{(n)} = e^{i\psi_{nB}}i(1 + e^{i\psi_n})\nu_n\sqrt{1-\nu_n^2}, \quad (15)$$

it is observed that frequencies corresponding to $\psi_n(\omega) = \pi + 2\pi p$ cannot pass through the filters. This fact is used to realize a way to obtain the desired properties of the filters by choosing:

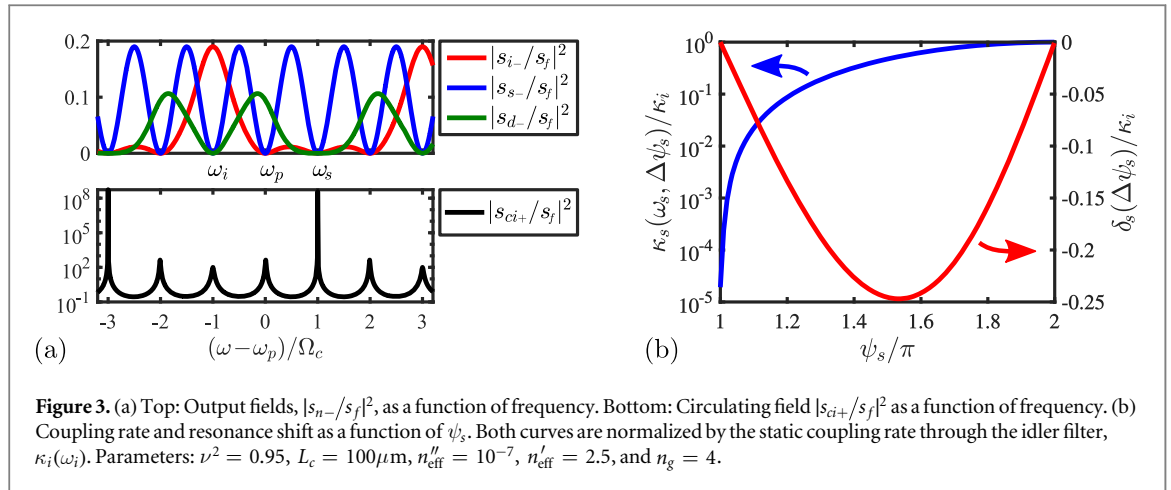


Figure 3. (a) Top: Output fields, $|s_{i-}/s_f|^2$, as a function of frequency. Bottom: Circulating field $|s_{ci+}/s_f|^2$ as a function of frequency. (b) Coupling rate and resonance shift as a function of ψ_s . Both curves are normalized by the static coupling rate through the idler filter, $\kappa_i(\omega_i)$. Parameters: $\nu^2 = 0.95$, $L_c = 100\mu\text{m}$, $n_{\text{eff}}^i = 10^{-7}$, $n_{\text{eff}}^s = 2.5$, and $n_g = 4$.

$$\psi_i(\omega_i) = 2\pi, \quad \psi_s(\omega_i) = \pi, \quad \theta_i(\omega_i) = \pi, \quad (16a)$$

$$\psi_s(\omega_s) = \pi, \quad \psi_i(\omega_s) = \pi, \quad \theta_i(\omega_p) = \pi. \quad (16b)$$

The conditions in (16) can be met by making the FSRs of the filters different integer values of Ω_c . Correspondingly, the path length differences should be different integer fractions of L_c as

$$\Delta L_i = L_c/4, \quad \Delta L_{di} = L_c/2, \quad \Delta L_s = L_c. \quad (17)$$

In figure 3(a) we plot the output fields (top panel) and the field circulating inside the storage ring (bottom panel) for these choices. From the top panel it is seen that $|s_{i-}|^2$ vanishes at ω_p and ω_s , and $|s_{s-}|^2$ goes to zero at ω_i , ω_p , and ω_s . We also plot the field in the drop port, $s_{d-} = D_{1,1}^{(i)} s_{i-}$, to show that it has no contributions from the signal and idler frequencies. From the bottom panel of figure 3(a), it is observed that the signal mode at ω_s is spectrally narrow compared to the idler and pump modes. This is caused by the choice $\psi_s(\omega_s) = \pi$, which corresponds to the signal filter being closed and the Q-factor only being limited by intrinsic loss. The design choices in equation (17) are thus seen to yield the desired filter properties.

The signal filter is tuned by modifying $\Delta\psi_s$. The corresponding change in the cavity-waveguide coupling is found from the tuning parameter ζ_s in equation (10). The amplitude of the matrix element $T_{2,2}^{(n)}$ describes the loss per round-trip of the intra-cavity field due to waveguide coupling. From equation (10) it is therefore seen that a coupling rate may be defined by $\exp[-\kappa_n \tau_{\text{RT}}] = |\zeta_n|$, or

$$\kappa_n(\omega, \Delta\psi_n) = -\frac{c}{n_g L_c} \ln[|\zeta_n(\omega, \Delta\psi_n)|], \quad (18)$$

where τ_{RT} is the cavity round-trip time. The resonances, ω_n , of the MZI-coupled ring are also affected by tuning $\Delta\psi_s$. They are found by the resonance condition on the round-trip phase of the MZI-coupled ring

$$\Phi_n(\omega_n) = \phi_c(\omega_n) + \arg[\zeta_i(\omega_n)\zeta_s(\omega_n)] = 2\pi. \quad (19)$$

In figure 3(b) we plot the coupling rate, κ_s , and resonance shift

$$\delta_s(\psi_s) = \omega_s(\psi_s) - \omega_s(\psi_s = \pi) \quad (20)$$

as a function of ψ_s . The coupling rate remains non-zero at $\psi_s = \pi$ due to the small imaginary part of the complex refractive index.

If the tunable phase, $\Delta\psi_s(t)$, has some time variation due to the electrical signal coming from the logic unit (see figure 1(a)), the coupling rate will also vary in time, $\kappa_s(t)$. The interference-based filtering of the MZI will work as long as $\Delta\psi_s(t)$ varies slowly relative to the propagation time through the MZI. In section 3 we use this fact to model the system as a single resonator with the signal mode having a time-dependent coupling rate. The resonance shift, δ_s , will be neglected by assuming that the chirp it induces on the signal photon does not affect its detection.

2.1. Frequency conversion

Since the storage ring has many modes separated by a FSR, signal and idler pairs are generated in spectral modes symmetrically distributed about the degenerate pump mode. By heralding on multiple idler modes, multiplexing in the frequency domain in addition to the time domain is possible [8]. With the choices of ΔL_n made here, any mode-pair satisfying

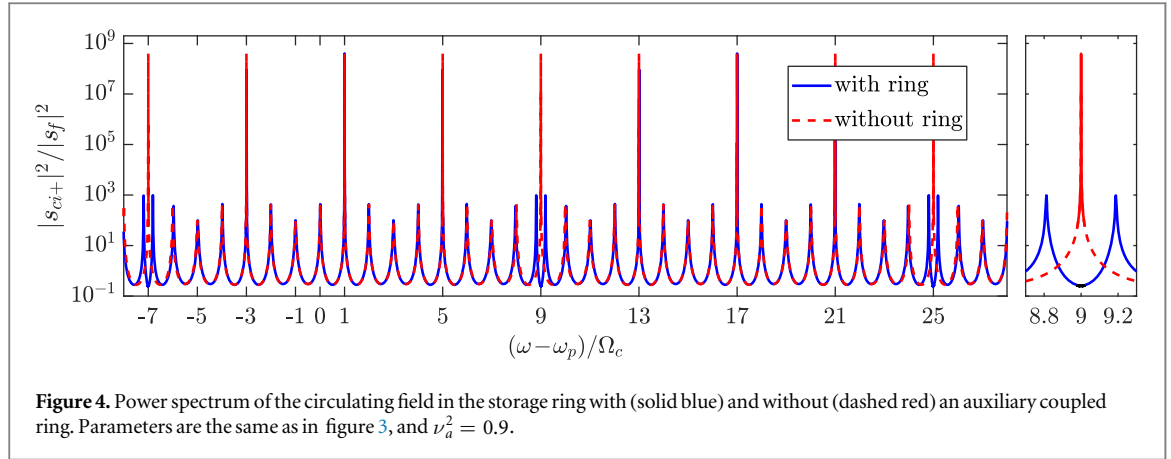


Figure 4. Power spectrum of the circulating field in the storage ring with (solid blue) and without (dashed red) an auxiliary coupled ring. Parameters are the same as in figure 3, and $\nu_a^2 = 0.9$.

$$\omega_s = \omega_p + (1 + 4p)\Omega_c, \quad \omega_i = \omega_p - (1 + 4p)\Omega_c, \quad p \in \mathbb{Z} \quad (21)$$

could be used. Multiplexing in frequency requires frequency conversion of signal photons to the target wavelength [8, 14]. If Bragg-scattering FWM [15] is used for the frequency conversion, the probability of up-conversion and down-conversion is equal (provided that phase-matching is uniform across several FSRs of the storage ring) [14, 16]. To overcome this symmetry, the storage ring can be coupled to an auxiliary ring with a length $L_r = L_c/16$ such that its resonances coincide with every fourth signal mode (see figure 2(b)). The ring-ring coupling will cause a splitting of the mode spectrum and thereby effectively eliminate either the up- or down-conversion cavity mode. To illustrate this, let us consider the auxiliary ring being coupled on the left side of the storage ring with a coupling region described by a matrix $C^{(t)}$ as in equation (2) (see inset in figure 2). The fields are then related by

$$s_{cs+} = \nu_a s_{ci-} + i\sqrt{1 - \nu_a^2} s_{a+}, \quad s_{a-} = i\sqrt{1 - \nu_a^2} s_{ci-} + \nu_a s_{a+}, \quad s_{a+} = e^{i\phi_a} s_{a-}, \quad (22)$$

where ν_a is the coupling coefficient of the directional coupler formed by the waveguide sections of each ring, and ϕ_a is the round-trip phase of the auxiliary ring. Solving equation (22) yields

$$s_{cs+} = \left(\nu_a - \frac{(1 - \nu_a^2) e^{i\phi_a}}{1 - \nu_a e^{i\phi_a}} \right) s_{ci-}. \quad (23)$$

Inserting equation (23) into (7) leads to a modified version of equation (10)

$$s_{ci+} = \frac{1}{1 - e^{i\phi_c} \zeta_i \zeta_s \left(\nu_a - \frac{(1 - \nu_a^2) e^{i\phi_a}}{1 - \nu_a e^{i\phi_a}} \right)} s_f. \quad (24)$$

In figure 4 we show the circulating field with and without the auxiliary ring coupled. Notice the splitting of the cavity modes at the suppressed frequencies

$$\omega_{\text{supp}} = \omega_p + (9 + 16p)\Omega_c, \quad p \in \mathbb{Z}. \quad (25)$$

Both the storage and auxiliary ring have a resonance at these frequencies and their coupling gives rise to two super-modes that are shifted away from the original resonances.

Detecting an idler photon at e.g. $\omega_i = \omega_p - 5\Omega_c$ heralds the presence of a signal photon at $\omega_s = \omega_p + 5\Omega_c$. Since the storage ring mode at $\omega_p + 9\Omega_c$ is now shifted, the signal can be down-converted to the target frequency $\omega_p + \Omega_c$ with high efficiency. In general, we can frequency-multiplex using all signal modes satisfying the relation

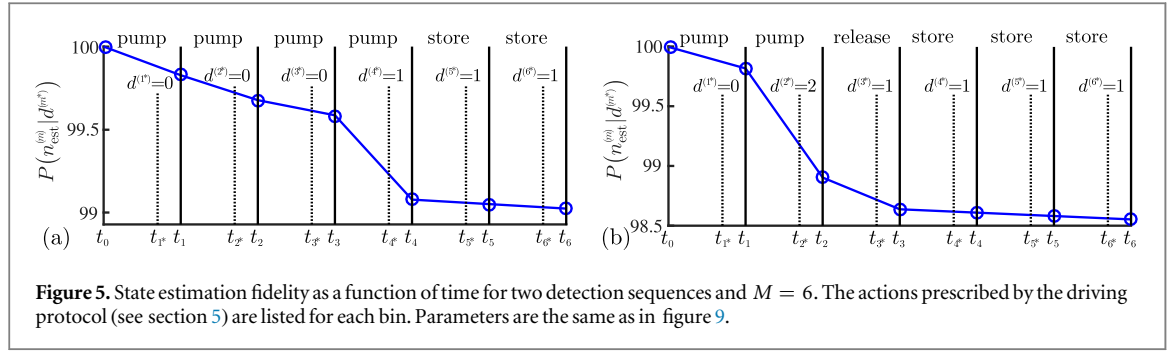
$$\omega_s = \omega_p + (5 + 8p)\Omega_c, \quad p \in \mathbb{Z}. \quad (26)$$

The fact that the signal photon is born inside the storage cavity (as opposed to the situation in [8, 14]) significantly simplifies the problem and near-unity conversion efficiency should be possible [16, 17].

If \mathcal{P} is the success probability of each frequency mode the total success probability from using N_F modes is $\mathcal{P}_{\text{tot}} = 1 - (1 - \mathcal{P})^{N_F}$, assuming perfect conversion efficiency and no reduction in temporal multiplexing efficiency of each frequency channel.

3. Temporal multiplexing model

The number of time bins available for multiplexing depends on the intrinsic decay rate of the storage ring, κ_L , and the speed of the feedback controls. The m th time bin is defined by the time interval $[t_{m-1}, t_m]$ and all bins



are assumed to be of equal length, $\tau_{\text{bin}} = t_m - t_{m-1}$. The feedback controls are the pump power, $|S_{\text{pump}}(t)|^2$, and signal filter phase, $\Delta\psi_s(t)$. The processing time of the logic unit, τ_D , determines the necessary lag between the time of deciding the action in bin $m + 1$, t_{m^*} , and its onset, $t_m = t_{m^*} + \tau_D$. If $N_I(t_m)$ and $N_S(t_m)$ denote the number of idler and signal detections up until t_m , the detection number is defined as

$$d^{(m)} \equiv N_I(t_m) - N_S(t_m). \quad (27)$$

We infer the state of the storage ring at t_m based on the value of the detection number at the decision time, t_{m^*} . For instance, $d^{(m^*)} = 1$ suggests that one signal photon occupies the cavity at t_m , which we denote as $n^{(m)} = 1$. If $d^{(m^*)} \geq 0$, the estimated number of signal photons is $n_{\text{est}}^{(m)} = d^{(m^*)}$. Since some idler photons might not be detected, the detection number can be negative and in this case we always pump the cavity and our estimation is therefore $n_{\text{est}}^{(m)} = d^{(m^*)} - d^{(m-1)}$.

The state estimation fidelity is the probability that our estimate of the state is correct and is given by

$$P(n^{(m)} = n_{\text{est}}^{(m)} | \mathbf{d}^{(m^*)}) = \frac{P(n^{(m)} = n_{\text{est}}^{(m)}, \mathbf{d}^{(m^*)})}{P(\mathbf{d}^{(m^*)})}. \quad (28)$$

The detection sequence $\mathbf{d}^{(m^*)} \equiv \{d^{(0)}, d^{(1)}, \dots, d^{(m-1)}, d^{(m^*)}\}$ contains information from all previous bins. We consider the photon generation successful only if the heralding efficiency (probability of having a single photon in the cavity conditioned on the given detection sequence) and the second-order correlation obey the threshold conditions

$$P(n^{(M)} = 1 | \mathbf{d}^{(M^*)}) \geq F_{\text{th}} \quad \text{and} \quad g^{(2)}(\mathbf{d}^{(M^*)}) \leq g_{\text{th}}^{(2)}, \quad (29)$$

where M enumerates the last bin of the emission cycle and $g^{(2)}(\mathbf{d}^{(M^*)})$ is defined by [18]

$$g^{(2)}(\mathbf{d}^{(M^*)}) = \frac{\sum_{n^{(M)}} n^{(M)} (n^{(M)} - 1) P(n^{(M)} | \mathbf{d}^{(M^*)})}{\left[\sum_{n^{(M)}} n^{(M)} P(n^{(M)} | \mathbf{d}^{(M^*)}) \right]^2}. \quad (30)$$

The thresholds F_{th} and $g_{\text{th}}^{(2)}$ are performance metrics of the source and can be chosen according to any application of interest. The success probability (probability that exactly one signal photon occupies the storage ring at t_M) is

$$\mathcal{P}(M) = \sum_{\mathbf{d}^{(M^*)}} P(n^{(M)} = 1, \mathbf{d}^{(M^*)}), \quad (31)$$

where the summation runs over all detection sequences fulfilling equation (29). Figure 5 illustrates two examples of detection sequences leading to successful state preparation. In figure 5(a), the detection of one idler photon in bin 4 heralds the presence of one signal photon and the state is stored until the end of the emission cycle. In figure 5(b), the detection of two idler photons in bin 2 leads to release of signal photons in bin 3. The detection of one signal photon in bin 3 suggests that the desired state is achieved and it is stored.

The system in figure 1(a) can be modeled by considering three modes of the storage ring where the control-phase of the signal filter, $\Delta\psi_s(t)$, is represented by a time-dependent coupling rate, $\kappa_s(t)$, for the signal mode as discussed in section 2. Photon pair generation is modeled using a Hamiltonian of the form

$$H_{\text{sys}} = \Delta_i \hat{a}_i^\dagger \hat{a}_i + \Delta_s \hat{a}_s^\dagger \hat{a}_s + \mathcal{X}(\hat{a}_i^\dagger \hat{a}_s^\dagger + \hat{a}_i \hat{a}_s), \quad (32)$$

where \hat{a}_s and \hat{a}_i are annihilation operators of the signal and idler modes, respectively. We use normalized units ($\hbar = 1$) and a classical pump rate described by \mathcal{X} , which is proportional to the nonlinear coefficient, $\chi^{(3)}$, and the energy of the pump cavity mode. Additionally, Δ_s and Δ_i are detunings between the pump frequency and the signal and idler modes, respectively. Coupling between the resonator and waveguides through the filters is modeled via collapse operators, $\hat{C}_{nL} = \sqrt{2\kappa_L} \hat{a}_n$, and $\hat{C}_n = \sqrt{2\kappa_n} \hat{a}_n$ with $n = i, s$ [19]. The loss rate, κ_L , of all modes is assumed equal. By neglecting self-induced nonlinear effects, the energy in the cavity follows from coupled mode theory [20]

$$\mathcal{X}(t) = \left| \int_{-\infty}^t e^{-\kappa_p(t-t')} S_{\text{pump}}(t') dt' \right|^2, \quad (33)$$

where the input power is assumed Gaussian, $|S_{\text{pump}}(t)|^2 \propto \exp[-(t - t_p)^2 / \tau_p^2]$. The pump width τ_p is 1ps and the time t_p is adjusted such that $\mathcal{X}(t_{m-1})$ is at least a thousand times smaller than its peak value.

The state of the storage ring, $|\psi(t)\rangle$, is calculated from equation (32) using a Monte Carlo method [19] with an initial state $|n^{(m-1)}, n_{ci}^{(m-1)} = 0\rangle$. The assumption of zero idler photons at t_{m-1} ($n_{ci}^{(m-1)} = 0$) is based on the coupling rate, κ_i , being much larger than the inverse bin duration, $1/\tau_{\text{bin}}$.

4. Probability analysis

We use Monte Carlo simulations [19] to evaluate the probability distribution $P(n^{(m)}, \mathbf{d}^{(m*)})$. The assumptions are: (1) detector dark counts are negligible. (2) The idler mode of the cavity is in the vacuum state at the beginning of each bin. (3) If $d^{(m*)} \leq 0$, then $n^{(m)} \leq 2$, which is a good approximation for the large detection efficiency used in our simulations. (4) The signal coupling rate, $\kappa_s(t)$, can be varied without increasing the loss rate, κ_L , which is equal for all three modes.

The probability $P(n^{(m)}, \mathbf{d}^{(m*)})$ is evaluated using an expansion

$$P(n^{(m)}, \mathbf{d}^{(m*)}) = \sum_{n^{(m-1)}} P(n^{(m)}, n^{(m-1)}, \mathbf{d}^{(m*)}) = \sum_{n^{(m-1)}} P(n^{(m)}, d^{(m*)} | n^{(m-1)}, \mathbf{d}^{(m-1)}) P(n^{(m-1)}, \mathbf{d}^{(m-1)}). \quad (34)$$

Notice that the probability distribution in the current bin m is updated using information from the total duration of the previous bins, $\mathbf{d}^{(m-1)}$, because the detector keeps acquiring information until the end of each bin. The second factor on the right-hand side (rhs) of equation (34) is found by a similar expansion, which means that the distribution $P(n^{(m)}, \mathbf{d}^{(m*)})$ can be found iteratively starting from the first bin

$$P(n^{(1)}, \mathbf{d}^{(1)}) = \sum_{n^{(0)}} P(n^{(1)}, d^{(1)} | n^{(0)}, d^{(0)}) P(n^{(0)}, d^{(0)}), \quad (35)$$

where $P(n^{(0)}, d^{(0)})$ is known since $n^{(0)}$ and $d^{(0)}$ both equal zero at the beginning of each emission cycle. Note that we omit an expansion over the initial state of the idler mode in equation (34) by assuming that it is in the vacuum state. In the following sections, it is explained how the probability distributions $P(n^{(m)}, d^{(m)} | n^{(m-1)}, \mathbf{d}^{(m-1)})$ and $P(n^{(m)}, d^{(m*)} | n^{(m-1)}, \mathbf{d}^{(m-1)})$ are calculated for pumping and releasing, respectively.

4.1. Pumping

If the cavity is pumped in bin m , the probability that there are $n^{(m)}$ signal photons in the cavity *and* the detection number is $d^{(m)}$ at t_m is

$$P_p(n^{(m)}, d^{(m)} | n^{(m-1)}, \mathbf{d}^{(m-1)}) = \sum_{n_i^{(m)}=I^{(m)}}^{\infty} P(d^{(m)} | n_i^{(m)}) P_p(n^{(m)}, n_i^{(m)} | n^{(m-1)}, \mathbf{d}^{(m-1)}), \quad (36)$$

where $n_i^{(m)}$ is the number of idler photons coupled through the idler filter between t_{m-1} and t_m . The subscript p is used to signify that we pump in bin m . The number of detected idler photons is $I^{(m)} = d^{(m)} - d^{(m-1)}$, because the signal filter is closed so no signal detections contribute to $d^{(m)}$. Note that the probability that the detection number equals $d^{(m)}$ only depends on $n_i^{(m)}$ and is given by

$$P(d^{(m)} | n_i^{(m)}) = \binom{n_i^{(m)}}{I^{(m)}} \eta^{I^{(m)}} (1 - \eta)^{n_i^{(m)} - I^{(m)}}, \quad (37)$$

where η is the detection efficiency. Since we only consider near-unity detection efficiency, we assume that the probability $P_p(n^{(m-1)} > 2 | d^{(m*)} \leq 0)$ is negligible and therefore truncate the summation in equation (34) after 2 for bins where we pump (this is the third assumption in the beginning of this section). The distribution $P_p(n^{(m)}, d^{(m*)} | n^{(m-1)}, \mathbf{d}^{(m-1)})$ is found by replacing $d^{(m)}$, $n_i^{(m)}$, and $I^{(m)}$ by $d^{(m*)}$, $n_i^{(m*)}$, and $I^{(m*)}$ in equations (36) and (37).

The probability of a certain configuration with $n^{(m)}$ photons in the signal mode and $n_i^{(m)}$ idler photons in the detector waveguide is found by projecting the state $|n^{(m)}, n_{ci}^{(m)}\rangle$ onto $|\psi(t_m)\rangle$ and tracing out the idler subspace for all Monte Carlo trajectories, where $n_i^{(m)}$ idler photons couple into the detector waveguide

$$P_p(n^{(m)}, n_i^{(m)} | n^{(m-1)}, \mathbf{d}^{(m-1)}) = \frac{1}{N_{\text{traj}}} \sum_{\text{traj}(n_i^{(m)})} \sum_{n_{ci}^{(m)}} \langle n^{(m)}, n_{ci}^{(m)} | \psi(t_m) \rangle^2. \quad (38)$$

Note that the probability is obtained by normalizing with the total number of trajectories N_{traj} . The probability $P_p(n^{(m)}, n_i^{(m*)} | n^{(m-1)}, \mathbf{d}^{(m-1)})$ is found by counting the number of idler collapses up until the time t_{m^*} instead of t_m .

With the time dependence of $|S_{\text{pump}}(t)|^2$ fixed, we can introduce the probability that at least one pair is created in bin m , $p^{(m)}$, as a generalized control setting for the pump. It is calculated using Monte Carlo simulations with the initial condition $|\psi(t_{m-1})\rangle = |0, 0\rangle$.

4.2. Releasing

If we release signal photons in bin m , the probability distribution $P_r(n^{(m)}, d^{(m)}|n^{(m-1)}, \mathbf{d}^{(m-1)})$ is also found using equations (36) and (37) with $I^{(m)}$ and $n_i^{(m)}$ replaced by $S^{(m)}$ and $n_s^{(m)}$, where $S^{(m)} = d^{(m-1)} - d^{(m)}$. Again, the subscript r indicates that we are releasing signal photons in bin m . The probability of different cavity states at t_m is given by the multinomial distribution

$$P_r(n^{(m)}, n_s^{(m)}|n^{(m-1)}, \mathbf{d}^{(m-1)}) = \frac{n^{(m-1)}!}{n_s^{(m)}! n^{(m)}! (n^{(m-1)} - n_s^{(m)} - n^{(m)})!} p_c^{n^{(m)}} p_s^{n_s^{(m)}} p_L^{n^{(m-1)} - n_s^{(m)} - n^{(m)}}. \quad (39)$$

The subscripts $\{c, s, L\}$ correspond to the cavity, signal waveguide, and environment loss channel, respectively. The probability that a photon remains in the cavity at time t is $p_c(t)$, the probability that it has coupled into the signal waveguide is $p_s(t)$, and $p_L = 1 - p_c - p_s$. The probabilities are found using rate equations for the ensemble average of the number operators

$$\begin{aligned} \frac{d\langle \hat{n}_c(t) \rangle}{dt} &= -2[\kappa_s(t) + \kappa_L] \langle \hat{n}_c(t) \rangle & \Rightarrow & p_c(t) = \exp\left(\int_{t_{m-1}}^t -2[\kappa_s(t') + \kappa_L] dt'\right), \\ \frac{d\langle \hat{n}_s(t) \rangle}{dt} &= 2\kappa_s(t) \langle \hat{n}_c(t) \rangle & & p_s(t) = \int_{t_{m-1}}^t 2\kappa_s(t') p_c(t') dt' \end{aligned} \quad (40)$$

where, e.g. $\langle \hat{n}_c(t) \rangle = n^{(m-1)} p_c(t)$, and the initial condition $p_c(t_{m-1}) = 1$ and $p_s(t_{m-1}) = p_L(t_{m-1}) = 0$ was used in equation (40). The distribution $P_r(n^{(m)}, n_s^{(m*)}|n^{(m-1)}, \mathbf{d}^{(m-1)})$ is found using the intermediary step

$$P_r(n^{(m)}, n_s^{(m*)}|n^{(m-1)}, \mathbf{d}^{(m-1)}) = \sum_{n^{(m*)}, n_s^{(m*)}} P_r(n^{(m)}, n_s^{(m*)}|n^{(m*)}, n_s^{(m*)}, n^{(m-1)}, \mathbf{d}^{(m-1)}) P_r(n^{(m*)}, n_s^{(m*)}|n^{(m-1)}, \mathbf{d}^{(m-1)}), \quad (41)$$

where the first factor on the rhs only depends on $n^{(m*)}$, such that

$$P_r(n^{(m)}, n_s^{(m*)}|n^{(m-1)}, \mathbf{d}^{(m-1)}) = \sum_{n^{(m*)}, n_s^{(m*)}} P_r(n^{(m)}, n_s^{(m*)}|n^{(m*)}) P_r(n^{(m*)}, n_s^{(m*)}|n^{(m-1)}, \mathbf{d}^{(m-1)}). \quad (42)$$

The distribution $P_r(n^{(m)}, n_s^{(m*)}|n^{(m*)})$ must be evaluated using equations (39) and (40) with the chosen temporal evolution of $\kappa_s(t)$.

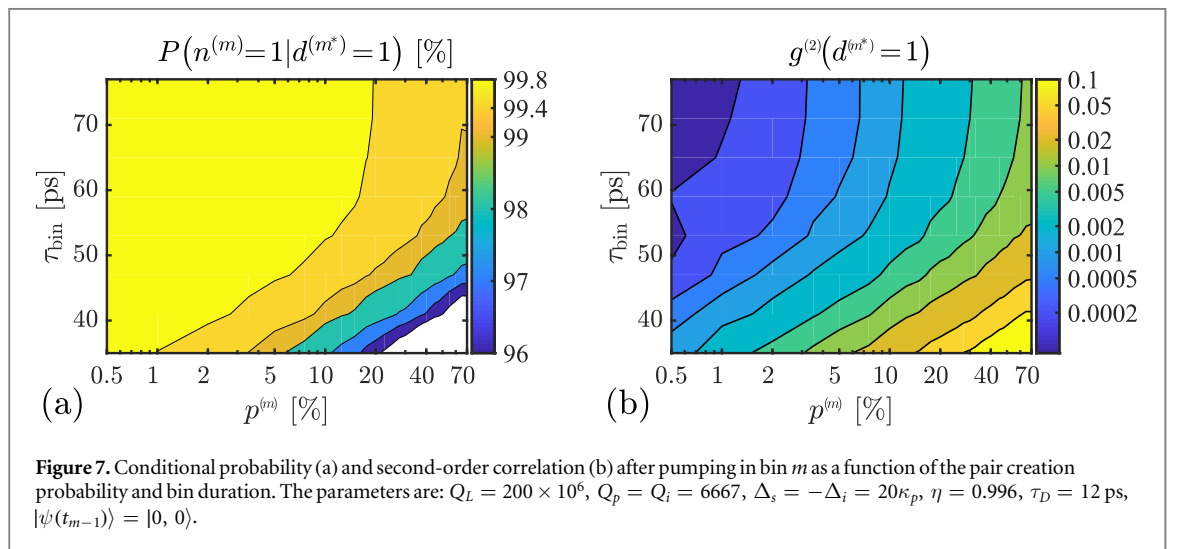
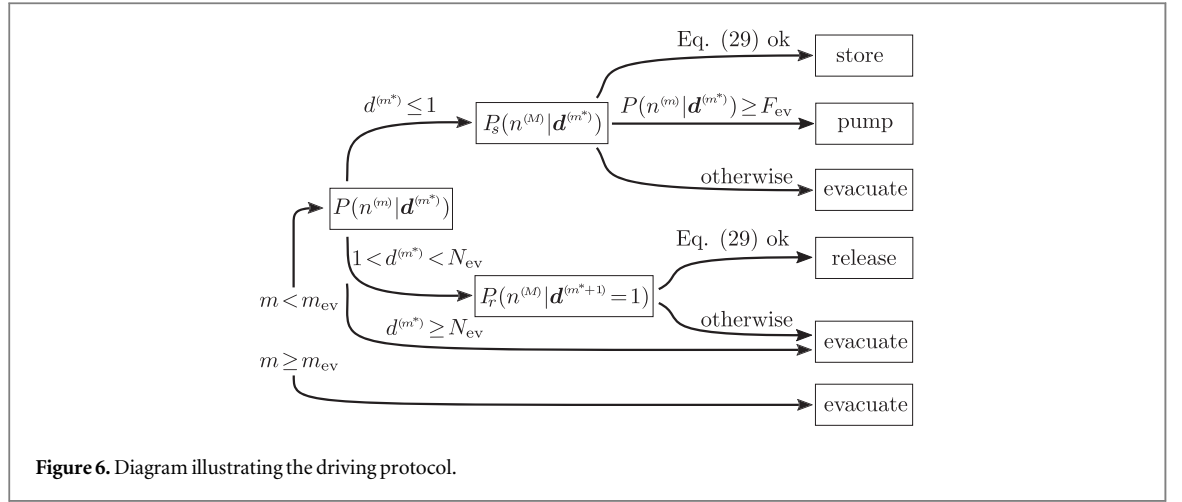
The faster signal photons couple into the waveguide, the smaller is the probability that they will be lost to the environment. If $p_c(t)$ drops instantly from 1 at t_{m-1} to its final value then such loss is avoided. This corresponds to $\kappa_s(t)$ being proportional to a Dirac delta distribution centered at t_{m-1} . However, the electrical signal that controls the signal filter has some finite temporal width. We assume its shape is Gaussian and that the temporal shape of the coupling is

$$\kappa_s(t) \propto \int_{t_{m-1}}^t e^{-\kappa_{\psi_s}(t-t')} e^{-(t'-t_r)^2/\tau_r^2} dt', \quad (43)$$

where $1/\kappa_{\psi_s}$ is a response time, t_r is adjusted such that $\kappa_s(t_{m-1})$ is at least a thousand times smaller than its peak value and the width, τ_r , is constrained by the condition $\kappa_s(t) \leq \kappa_i$ seen in figure 3(b). With the shape of $\kappa_s(t)$ given by equation (43), the release control setting is completely determined by the value $p_c^{(m)} \equiv p_c(t_m)$ calculated from equation (40).

5. Driving protocol

The driving protocol relates information from photon detections to control actions. Figure 6 depicts which actions are taken in bin $m + 1$ depending on the updated probability distribution in bin m , $P(n^{(m)}|\mathbf{d}^{(m*)})$. In some parameter regimes, it turns out to be advantageous to evacuate the cavity after a certain number of bins, m_{ev} , irrespective of the state estimation fidelity. If $m < m_{\text{ev}}$, the protocol depends on $\mathbf{d}^{(m*)}$ in the following way: for $d^{(m*)} \leq 1$, we evaluate the distribution at the emission time in case the state is stored until then, $P_s(n^{(M)}|\mathbf{d}^{(m*)})$. If equation (29) is fulfilled, the state is stored. If not, the next bin is pumped if the fidelity of our current state estimation is larger than the control parameter F_{ev} and otherwise evacuated. For $1 < d^{(m*)} < N_{\text{ev}}$, we calculate the distribution $P_r(n^{(M)}|\mathbf{d}^{(m*+1)} = 1)$ corresponding to a release in the next bin followed by storage until the emission time. Again, if the threshold conditions are met by evaluating equation (29), we release in the following bin and evacuate otherwise. N_{ev} is a control parameter that primarily serves to reduce the optimization space. However, it also allows us to eliminate release from the protocol by choosing $N_{\text{ev}} = 2$.



In the following sections we provide more details about the protocol in case of pumping and releasing, respectively.

5.1. Pumping protocol

When pumping in bin m , we assume that it is advantageous to keep the pump power below a level, which for the initial condition $|\psi(t_{m-1})\rangle = |0, 0\rangle$ results in a distribution $P_s(n^{(M)}|\mathbf{d}^{(m*)})$ that obeys the requirements in equation (29). It is given by

$$P_s(n^{(M)}|\mathbf{d}^{(m*)}) = \sum_{n^{(m)}=n^{(M)}}^{\infty} P_s(n^{(M)}|n^{(m)}, \mathbf{d}^{(m*)})P(n^{(m)}|\mathbf{d}^{(m*)}), \quad (44)$$

where the subscript s indicates storage until t_M . The probability that there are $n^{(M)}$ signal photons in the cavity at t_M given there was $n^{(m)}$ at t_m is given by equation (39) with $p_s = n_s = 0$

$$P_s(n^{(M)}|n^{(m)}, \mathbf{d}^{(m)}) = P_s(n^{(M)}|n^{(m)}) = \frac{n^{(m)}! p_c^{n^{(M)}} (1 - p_c)^{n^{(m)} - n^{(M)}}}{n^{(M)}! (n^{(m)} - n^{(M)})!}, \quad (45)$$

where $p_c = \exp[-2\kappa_L(t_M - t_m)]$ is the probability that a photon remains in the cavity until t_M .

Figure 7 shows how the relevant properties of the distribution $P(n^{(m)}|\mathbf{d}^{(m*)})$ in equation (44) vary as a function of the pump control setting, $p^{(m)}$, and bin duration, τ_{bin} . For small τ_{bin} , our state estimation fidelity is degraded by the finite probability that idler photons remain inside the cavity. As the bin duration is increased, the fidelity eventually becomes dominated by the detection efficiency and the contours become vertical. This suggests that there must be an optimum bin duration, because increasing it allows larger pump power while reducing the total number of bins. The properties illustrated in figure 7 apply to any bin, but since $P_s(n^{(M)}|\mathbf{d}^{(m*)})$ depends on $M - m$, the maximum control setting for the pump must be evaluated for each bin.

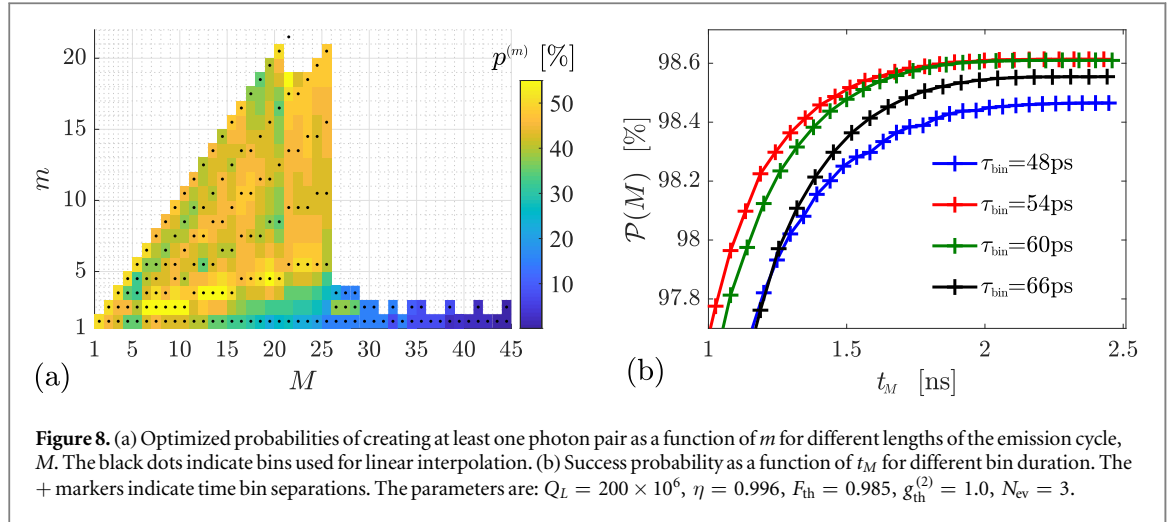


Figure 8. (a) Optimized probabilities of creating at least one photon pair as a function of m for different lengths of the emission cycle, M . The black dots indicate bins used for linear interpolation. (b) Success probability as a function of t_M for different bin duration. The + markers indicate time bin separations. The parameters are: $Q_L = 200 \times 10^6$, $\eta = 0.996$, $F_{th} = 0.985$, $g_{th}^{(2)} = 1.0$, $N_{ev} = 3$.

5.2. Release protocol

To test whether releasing in bin m can lead to a successful state creation, the success conditions in equation (29) can be evaluated using equation (44) for all possible outcomes $\{n^{(m)}, d^{(m*)}\}$ with a fixed control setting $p_c^{(m)}$. If equation (29) can be fulfilled, the control setting is adjusted to maximize the success probability. Since we are only interested in the high detection efficiency regime, we assume that only $d^{(m*)} = 1$ provides a sufficiently large state fidelity and therefore only use the outcomes $\{n^{(m)}, 1\}$ to optimize the control setting. If equation (29) cannot be met, the cavity is evacuated. Determining whether it is advantageous to release or evacuate requires an evaluation of the success probability for a very large number of outcome scenarios. We therefore simplify the release protocol by always evacuating if $d^{(m*-1)} \geq N_{ev}$.

While the optimization procedure described above is done numerically, insight into the maximum success probability of the release process may be gained by considering the probability that $n^{(m+1)} = 1$ after releasing in bin $m + 1$. It is given by equation (39)

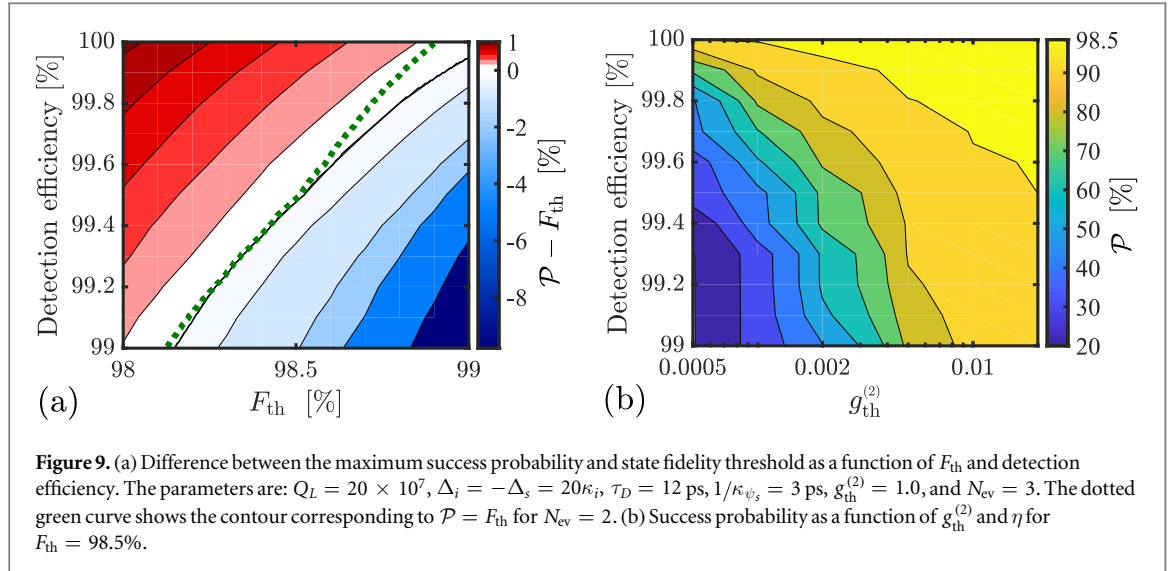
$$\begin{aligned}
 P(1|n^{(m)}, \mathbf{d}_r^{(m*)}) &= \sum_{n_s^{(m)}=0}^{n^{(m)}-1} \frac{n^{(m)}! p_c p_s^{n_s^{(m)}} p_L^{n^{(m)}-1-n_s^{(m)}}}{n_s^{(m)}!(n^{(m)}-1-n_s^{(m)})!} = n^{(m)} p_c \sum_{n_s^{(m)}=0}^{n^{(m)}-1} \binom{n^{(m)}-1}{n_s^{(m)}} p_s^{n_s^{(m)}} p_L^{n^{(m)}-1-n_s^{(m)}} \\
 &= n^{(m)} p_c (p_s + p_L)^{n^{(m)}-1} = n^{(m)} p_c (1 - p_c)^{n^{(m)}-1}.
 \end{aligned} \tag{46}$$

The maximum is found when $n^{(m)} p_c = 1$ and equals $1/2$ for $n^{(m)} = 2$ and $4/9$ for $n^{(m)} = 3$. For perfect detectors this illustrates that the probability of reaching a single photon state after initially creating two or three pairs is rather good.

5.3. Optimization of protocol

To optimize the protocol, we start by assuming there is only a single time bin available and iteratively increase M while keeping track of the success probability. When evacuating in bin m , the optimum strategy for the remaining $M - m$ bins is known from a previous iteration. The contribution to the overall success probability is $P(\mathbf{d}^{(m*-1)})P(M - m)$, where $\mathbf{d}^{(m*-1)}$ is the detection sequence leading us to evacuate in bin m . For instance, for $M = 3$ there is a possibility that $\mathbf{d}^{(1*)}$ causes us to evacuate the cavity in bin 2. In this scenario, we treat the last bin as the $M = 1$ case because the initial condition of bin 3 will be $|\psi(t_2)\rangle = |0, 0\rangle$ after evacuation. The protocol parameters for the last bin are then set as the optimum parameters found for $M = 1$. The iteration continues until equation (29) cannot be met for larger M . An upper bound on M is found by considering that F_{th} must be larger than the probability that a signal photon remains in the cavity for M bins, $\exp[-2\kappa_L M \tau_{bin}]$. A fixed pump sequence, $\mathbf{p}^{(M)} \equiv \{p^{(1)}, p^{(2)}, \dots, p^{(M-1)}, p^{(M)}\}$, is used for all detection sequences $\mathbf{d}^{(M)}$ unless an evacuation occurs in bin $m < M$. The single bin probability distribution in equation (38) has been found using Monte Carlo simulations as a function of $p^{(m)}$ for the discrete set of values $p^{(m)} \in [0.1, 0.2, 0.5, 1, 2, 3.5, 5 - 50, 55, 60, 65, 70]$, where the step-size between 5 and 50 is 2.5 and all numbers are given in %.

All the control parameters N_{ev} , F_{ev} , m_{ev} , and $\mathbf{p}^{(M)}$ are optimized for each M to maximize the success probability. Additionally, $p_c^{(m)}$ is optimized for each bin and τ_{bin} is optimized for the entire emission cycle. Figure 8(a) shows an example of the optimized pump sequences. For each M on the horizontal axis, the vertical axis plots the sequence $\mathbf{p}^{(m)}$ with colors indicating the value of $p^{(m)}$. For $M > 20$, the cavity is always evacuated in a bin m , for which $m < M$. For $M > 25$, the optimum strategy is to evacuate at $m = m_{ev}$ and the number of colored bins is given by $m_{ev} - 1$. As the number of possible pump sequences increases exponentially with M , we



optimize using a small sample of bins and use linear interpolation to find $p^{(m)}$ for all bins. The black dots indicate which bins are used in the interpolation. Figure 8(b) shows how the optimized success probability depends on the bin duration. The optimum choice for τ_{bin} is seen to correspond to where the contour lines in figure 7(a) start to become vertical. It seems reasonable that longer bins are sub-optimal because figure 7 suggests that no benefit from increased pump power is possible.

6. Simulation results

The system performance is evaluated by fixing the static coupling- Q of the idler and pump cavity modes at $Q_n = \omega_n/2\kappa_n = 6667$ ($n = i, p$) and optimizing the success probability for loss rates corresponding to intrinsic quality factors of 40, 80, and 200 million. Figure 9(a) shows the trade-space between the state fidelity threshold and success probability at different detection efficiency for $Q_L = 200 \times 10^6$ and $g_{\text{th}}^{(2)} = 1.0$ (this large value of $g_{\text{th}}^{(2)}$ ensures that it does not limit the success probability). Remarkably, a success probability and state fidelity of 99% is achievable for η just below unity. Alternatively, a 99% state fidelity is achieved with a success probability of $\mathcal{P} = 89.2\%$ if $\eta = 0.99$. Note that $\mathcal{P} > F_{\text{th}}$ is possible because some detection sequences result in a state fidelity larger than the threshold. Figure 9(b) shows the effect of reducing the second-order correlation threshold for $F_{\text{th}} = 98.5\%$. It illustrates the reduction in success probability when requiring a lower multi-photon contamination level.

We investigated the detrimental effect of increasing the loss rate and how performance can be restored using frequency multiplexing. Figure 10(a) shows the contour lines $\mathcal{P} = F_{\text{th}}$ for three different values of Q_L . In figure 10(b) we plot the success probability with $F_{\text{th}} = 99\%$ as a function of detection efficiency. Figure 10(b) also shows the necessary number of parallel frequency modes to achieve a total success probability of $\mathcal{P}_{\text{tot}} = 99\%$. For instance, reducing Q_L from 200 to 40 million only requires 4 frequency modes to restore \mathcal{P}_{tot} for $\eta = 1$.

7. Discussion

Our analysis shows that heralded single photon sources should be possible by on-chip multiplexing with near-unity purity. However, the device requirements are stringent—especially on the detector and feed-forward.

State of the art demonstrations of chip-integrated resonators [21–23] have reached quality factors exceeding 200 million, showing that the required intrinsic quality factors are within reach. For our protocol, the storage ring round-trip time should be much shorter than the pump pulse duration. Practically, this means that the storage ring should be less than ~ 100 μm in circumference. Larger devices with longer pump pulses can be used at the cost of reducing the number of available time bins.

The only detector technology that is currently able to approach the performance requirements are superconducting nanowire single photon detectors (SNSPDs) [24–28]. Electronic logic [29] and electro-optic switching [30] have been demonstrated at cryogenic temperatures, which are necessary when using SNSPDs and assuming a control set-time, τ_D , on the order of 10 ps.

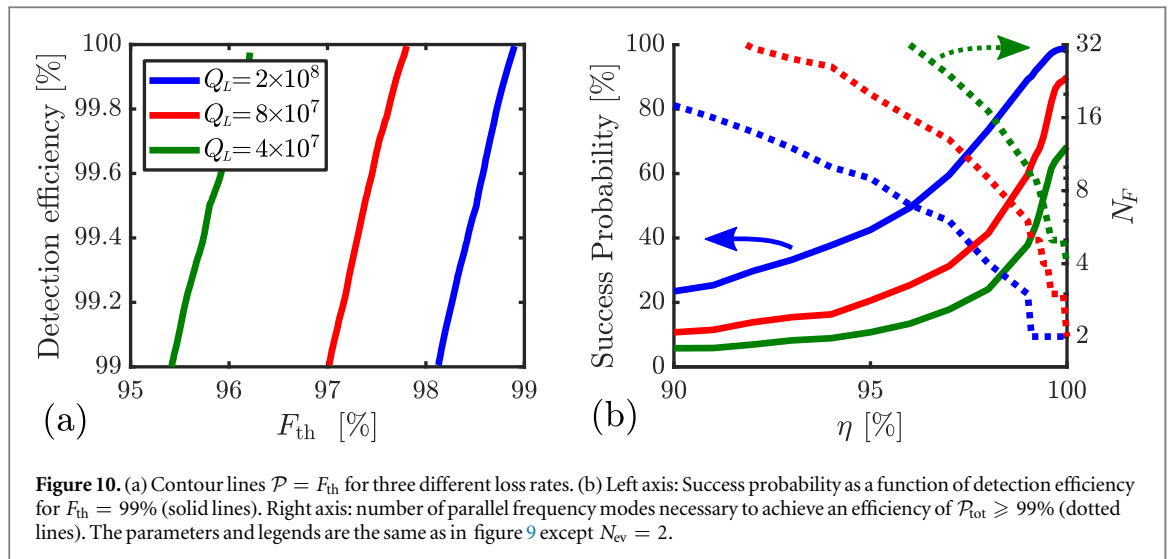


Figure 10. (a) Contour lines $\mathcal{P} = F_{th}$ for three different loss rates. (b) Left axis: Success probability as a function of detection efficiency for $F_{th} = 99\%$ (solid lines). Right axis: number of parallel frequency modes necessary to achieve an efficiency of $\mathcal{P}_{tot} \geq 99\%$ (dotted lines). The parameters and legends are the same as in figure 9 except $N_{ev} = 2$.

As seen from figure 9(a), the performance is not significantly reduced if the release step is omitted ($N_{ev} = 2$). This means that the tunable signal filter only needs to be low-loss in its closed state since loss during evacuation is irrelevant. In comparison, switches for spatial multiplexing must be low-loss in both states. The tunable output filter must, however, be low-loss in both settings. Since the output filter is only used for emission (once per emission cycle), one might consider using two different physical mechanisms to tune $\Delta\psi_s$ and $\Delta\psi_o$, such as carrier dispersion and heating. Developments in reducing the thermal response time in nanophotonic structures [31] could be a path towards high-speed low-loss switching.

Using cavity modes with different coupling rates for the idler, pump, and signal has been shown to enable signal-idler states with joint spectral amplitudes that are almost completely separable (implying high purity signal states) [32, 33]. The main challenges for creating indistinguishable photons with our proposed architecture is stabilization of the high Q resonance and repeatability of the output filter opening. The purity and temporal shaping of photons emitted from our proposed architecture will be studied in more detail in future work.

In conclusion, near-unity efficiency and photon purity is achieved by Bayesian inference, based on known system parameters and photon detections; similar Bayesian state estimation should also be useful for improving bulk-optics multiplexed sources [6, 7] and relative-multiplexing schemes [34]. This proposal of near-perfect on-chip single photon sources substantiates the feasibility of quantum technologies that require the production of large-scale photonic quantum states, such as optical quantum repeater networks, precision measurements, and quantum computing systems.

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